Economics

Impact of the Average Tax Rate on the Aggregate Demand (Keynesian Models)

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ABSTRACT. Based on an analysis of a modified version of the standard Keynesian Model of a product market, it is shown that a change in the average tax rate has a complex effect on aggregate demand. Depending on the marginal propensity of households to consume and the marginal propensity for government purchases, an increase in the average tax rate may lead to either a decrease or an increase in aggregate demand. In this case, since the parameter of marginal propensities to purchase is easily regulated, by selecting its appropriate value the government can purposefully use a tax increase to stimulate or to reduce aggregate demand. © 2012 Bull. Georg. Natl. Acad. Sci.

Key words: Keynesian model of aggregate demand, average tax rate, marginal propensity to consume, marginal propensity to public purchases.

Since the 1930s, after John Maynard Keynes proposed the concept of government regulation of the economy, economists' interest in taxes has grown considerably. As we know, in this concept, taxes, along with government purchases and transfer payments, are supposed to play a significant role in regulating aggregate demand and, through aggregate demand, in solving problems of employment, inflation, and economic growth.

In contemporary macroeconomics, the interrelation of taxes and aggregate demand is ambiguously defined: it is thought that increasing taxes has a negative effect on aggregate demand and that lowering them has a positive effect, since the main element of aggregate spending – the amount of household consumer spending – decreases in the former case and increases in the latter [1, ch. 3; 2, ch. 9; 3, ch. 12; 4, ch. 5]. However, because every phenomenon, including a change in taxes, has two sides – positive and negative – by considering the relationship between taxes and aggregate demand only in this context, we significantly simplify the existing reality. It can be shown that, in a certain situation, a tax increase causes an increase in aggregate demand and a tax cut causes a decrease [5]. We will consider this question in greater detail.

Version I of the Keynesian Model. The explanation of the mechanism and pattern of the average tax rate's influence on aggregate demand is traditionally based on using a modeling method. We will turn to this method and first consider the simplest standard Keynesian Model of equilibrium in the market for goods and services, which can be written as follows [1-4]:

$$E = C + I + G + NX , \qquad (1)$$

$$C = a + b(Y - T), \qquad (2)$$

$$I = I_0, \ G = G_0, \ NX = NX_0,$$
 (3)

$$T = T(Y), \tag{4}$$

$$Y = E , (5)$$

where *E* is aggregate spending; *C* is household consumption; *I* is gross domestic private investments; *G* is government purchases; *NX* is net exports; *a* is autonomous consumption; *b* is marginal propensity of households to consume, $0 \le b \le 1$; *T* is net taxes (the difference between taxes and transfers); and *Y* is gross domestic product (GDP).

In this system, conditions (1)–(4) determine aggregate spending. According to (2), the element *C* of this spending is a linear function of current disposable income (Y - T). As for the remaining three elements, *I*, *G*, and *NX*, for the sake of simplicity it is understood that they are given exogenously in the model and fixed at the levels I_0 , G_0 , and NX_0 , respectively, as indicated in (3).

The condition corresponding to net taxes (4) requires special scrutiny. Traditionally, in a simple model such as (1)–(5) it is either accepted that taxes are of a lump-sum nature (or fixed), and $T = T_0$, where T_0 is a fixed amount, or a linear taxation system is considered, in which *T* is defined as a linear function of *Y*. In the latter case, depending on what form of taxation T(Y) describes, three possible versions can be considered: functions corresponding to proportional, linearly progressive, and linearly regressive taxation. We should point out that in model (1)–(5), the consideration of any of the functions given here in the role of T(Y) makes it possible to draw almost the same conclusions. Therefore, we will dwell on just one of them, for example,

$$T(Y) = tY. (6)$$

Henceforth we will call the system (1)–(6) *Version I of the Keynesian Model.*

Taking into account conditions (2), (3), and (6), in (1) we get:

 $E = b(1-t)Y + I_0 + G_0 + NX_0 + a .$

With a fixed level of prices (which takes place in the model under consideration), E, which is determined by the given equation, can be regarded as the value of aggregate demand. As we see, E depends on the aggregated average tax rate t and, all else being equal, decreases in relation to the latter. In turn, in model (1)–(6), for a given fixed level of prices, the output (supply) of GDP amounts to Y. This implies that it is completely determined by aggregate demand.

In such conditions, the value of equilibrium GDP is determined from the equilibrium equation of the market for products and services (5):

$$Y = \lambda_1 A_1, \tag{7}$$

where A_1 is the amount of autonomous spending:

$$A_1 = a + I_0 + G_0 + NX_0, (8)$$

and λ_1 is autonomous spending multiplier:

$$\lambda_1 = \frac{1}{1 - b(1 - t)}.$$
(9)

Since the multiplier λ_1 decreases in relation to *t*, (7)–(9) formally lead to the following conclusions:

1. For given autonomous spending (all else being equal), equilibrium output is a decreasing function of t. At the same time, if we assume that t can take extreme values from 0 to 1, then the equilibrium output is maximum when t = 0 and minimum when t =1. In particular, $Y_{max} = A_1/(1-b)$ and $Y_{min} = A_1$.

2. For given autonomous spending, the net budget revenues (net taxes T) corresponding to equilibrium output are an increasing function of t. T is maximum when t = 1 and minimum when t = 0. In this case, $T_{max} = A_1$ and $T_{min} = 0$. 3. For given *t*, the equilibrium output and corresponding budget revenues increase (or decrease) when there is an increase (or decrease) in autonomous spending A_1 , of which one of the elements is government purchases G_0 .

We should point out that a change, an increase, for example, in A_1 causes simultaneous upward movement of the curves corresponding to T and Y.

With aggregate supply that does not depend on t, which takes place in model (1)–(6), the relationship between the average tax rate, equilibrium output, and budget revenues can be considered true only when government purchases G_0 and net taxes T do not depend on each other. Naturally, in such conditions, when the average tax rate rises and G_0 is fixed, there is an outflow of some funds from economic circulation, which, all else being equal, has a negative effect on the amount of aggregate demand and causes a contraction of equilibrium output.

However, in reality, T and G are quantities that depend on each other. In practice, the value of G is generally planned, for the most part, depending on what the expected net tax revenues T are. Furthermore, the need for changes in the average tax rate t is determined precisely by the steady growth of government purchases. According to Wagner's law, demand for public goods rises faster than demand for private goods, which is gradually saturated [6]. Therefore, consumers are willing to give up more and more of their income as taxes funding the production of public goods [7, p. 390]. Hence, in the model of aggregate demand, G and T should be considered not as isolated from each other – as in (1)–(6) – but as related to each other.

Version II of the Keynesian Model. We now consider the connection between government purchases (G)and net taxes (T) using an equation for the government's budget:

$$D = G + rB_{-1} - T = (G - T) + rB_{-1},$$
(10)

where B_{-1} is the amount of government debt or government assets at the beginning of the period (in the case of debt, $B_{-1} > 0$; in the case of assets, $B_{-1} < 0$; r is the averaged rate based on which interest payments are made at the expense of debt or assets. Consequently, rB_{-1} represents the amount of debt service ($rB_{-1} > 0$) or interest income ($rB_{-1} < 0$) received from payments out of assets; and D is a quantity representing the budget's deficit or surplus. If D = 0 in (10), then the budget is balanced. If D < 0, then the budget has a surplus. And finally, if D > 0, then the budget has a deficit.

In the case of a deficit budget, tax revenues are not enough to cover spending. Therefore, the government is forced to borrow an appropriate amount from the private sector, international financial organizations, other countries, or the central bank. Borrowing from the private sector is particularly common. This process is carried out directly by the state treasury, whose securities are sold to individuals, firms, commercial banks, and other financial institutions. The money obtained in this way at the expense of the state treasury is used, just the way tax revenues are, to cover government spending. Financing a deficit with credit from the private sector (debt financing) is the basic form of deficit financing and is widely used in most countries in the current conditions. However, there are individual exceptions, especially in developing countries, when the treasury borrows from the central bank to finance a deficit. In this case, the central bank actually purchases an appropriate part of the treasury's debt and creates "high-efficiency money" [3, ch. 9]. As we know, such financing is called monetization of the deficit. Without dwelling here on the positive and negative points of financing a budget deficit in these ways, we only point out that a budget cannot be constantly in deficit. There are periods when it is in surplus. In such cases, the government uses the surplus to repay or reduce the accumulated debt, or to create a reserve fund.

For simplicity, in what follows we use D to represent a deficit and B to represent government debt. At the same time, if necessary, we will specify the content of these quantities more precisely.

Equation (10) shows that the total budget deficit D is divided into two parts. One of them (G - T) is called a *primary deficit* when it is positive, and a *positive primary balance* when it is negative; and the other, rB_{-1} , is net interest payments [1, ch. 16]. Representing the deficit in this form emphasizes the special significance of government debt service in budget spending. If there is debt, the interest payments necessary to service it may be so high that the budget as a whole is in deficit, even in the case of a positive primary balance.

As we see, the amount of government debt at the beginning of the period determines how much the current budget is in deficit. For its part, the budget deficit is also a basis for the origin and growth of debt. Or rather, a budget deficit in the current period fosters the growth of government debt at the beginning of the next period. In general, the following relationship is valid [4, p. 557]:

 $B = B_{-1} + D ,$

where B_{-1} and B are the values of government debt at the beginning and end of the period, respectively.

In this relationship we take into account the value of D from (10). Using simple operations, we get an equation that can be used to determine government debt based on the primary budget deficit as:

$$B = (G - T) + (1 + r)B_{-1}.$$
 (11)

We will assume that B_{-1} in (11) is fixed and is a given quantity. This is a natural assumption, since the amount of B_{-1} is completely determined by decisions that the government has made in past periods. We will also assume that the value of the debt *B* at the end of the period is exogenously planned in the government budget and, if necessary, can be changed by taking on new debt or reducing current spending. As for government purchases *G*, they are tied to *T* and are determined from (11) as follows:

$$G = T + (B - (1 + r)B_{-1}).$$
(12)

Consequently, we understand that the amount of government purchases is determined, on the one

hand, by net tax revenues T and, on the other hand, by the policy that is conducted in relation to government debt. In other words, a change in G cannot be isolated – in the form in which it is traditionally considered in simple Keynesian Models, including the model (1)–(6) – and it is always associated with a change in taxes or debt (or both at the same time).

We replace the condition $G = G_0$ in model (1)– (6) with (12), and we call the system modified in this way *Version II of the Keynesian Model*. The equation for calculating equilibrium output will take the following form for this model:

$$Y = \lambda_2 A_2, \tag{13}$$

where

$$A_{2} = a + (B - (1 + r)B_{-1}) + I_{0} + NX_{0}, \qquad (14)$$

$$\lambda_2 = \frac{1}{1 - b(1 - t) - t}.$$
(15)

Consequently, in (13)–(15), in contrast to (7)–(9), what determines autonomous spending A_2 , along with other elements, is not total government purchases G_0 , but only the part of them made at the expense of government debt incurred in the current period $(B - (1+r)B_{-1})$. According to (11), this quantity is determined by the primary budget deficit (G - T). Moreover, in Version II of the Keynesian Model, the autonomous spending multiplier λ_2 has a completely different form. While in conditions (7)– (9) the multiplier λ_1 diminishes in relation to *t*, the opposite situation takes place in this case, and the multiplier λ_2 increases in relation to *t*. This circumstance leads to the following conclusions for Version II of the Keynesian Model:

1. All else being equal, the creation or growth of government debt (creation or growth of a primary budget deficit (G - T)) has a positive effect on equilibrium output, while reduction of government debt or growth of government assets (creation or growth of a primary budget surplus (T - G)) has a negative

effect. It is obvious that this situation is completely consistent with traditional Keynesian theory.

2. All else being equal, equilibrium output is an increasing function of the average tax rate *t*: dY/dt > 0. For given positive autonomous spending: $Y_{min} = A_2/(1-b)$, when t=0; and $Y_{max} = \infty$, when t=1. This result, which is not the customary one for Keynesian theory, is interesting from the point of view that, according to Version II of the Keynesian Model, in conditions of insufficient autonomous spending, one of the most important ways of increasing aggregate demand and boosting economic activity is to increase the average tax rate.

3. All else being equal, net budget revenues are an increasing function of t, and for given $A_2 > 0$: $T_{min} = 0$, when t = 0; and $T_{max} = \infty$, when t = 1.

We dwell further on an interesting result that follows from the relationship (13)-(15). In characterizing the effectiveness of fiscal policy tools, researchers often turn to the theorem of the well-known economist Trygve Haavelmo [8; 9, p. 95]. Based on a simple Keynesian Model in which taxes are determined independently of Y, the theorem asserts that the balanced budget multiplier is equal to zero. In other words, according to this theorem, if the government increases its purchases and taxes by the same amount $\Delta G = \Delta T$, then output will rise by the same amount, that is, the equality $\Delta G = \Delta T = \Delta Y$ will be fulfilled. It can be shown that this theorem is also valid in Version II of the Keynesian Model (It is not possible to prove the validity of this theorem based on Version I of the Keynesian Model, or model (1)-(6), since government purchases and taxes are not a priori interrelated in it).

Consequently, according to Version II of the Keynesian Model, all else being equal, a tax increase fosters growth of output, but the overall effect obtained in this way is used only to provide for government purchases (the amount of household consumption remains unchanged, in spite of the growth of output; and investments and net exports are also unchanged, since, according to the assumption, these characteristics are given exogenously in the model and they are fixed).

To clarify why equilibrium output is increasing in relation to the tax rate in Version II of the Keynesian Model, we will first explain the principle of operation of the multiplier λ_2 . We will use the standard method and consider a situation in which the amount of autonomous spending A_2 increases by one unit. This change will cause a multistage process in each stage of which the equilibrium output and the income corresponding to it will grow by a certain amount. In keeping with these stages, we will designate the value of the corresponding increases as $\Delta Y^{(1)}$, $\Delta Y^{(2)}$, $\Delta Y^{(3)}$, and so on.

It is clear that for the first stage $\Delta Y^{(1)} = 1$. From this unit increase of income, (1 - t) will remain in the private sector, and the other part (*t*) will go to the government's budget in the form of taxes.

In the second stage, households use the part b(1-t) of their disposable income (1-t) for consumption, which leads to growth of equilibrium output by the same amount. In parallel, the revenue t that the budget receives goes out into the market for goods and services and increases the equilibrium output by the amount t. So in the second stage the total increase in equilibrium output will be $\Delta Y^{(2)} = b(1-t) + t$. It should be noted that, as follows from what was said above, [b(1-t) + t] expresses spending by households and the government to purchase products and services from a unit of income additionally created in the economy. Therefore, [b(1-t)+t] represents the joint marginal propensity of households and the government to purchase products and services.

Considering this circumstance, it is easy to see that for the third stage:

 $\Delta Y^{(3)} = [b(1-t)+t]\Delta Y^{(2)} = [b(1-t)+t]^2.$

The increments of equilibrium output corresponding to subsequent stages are obtained analogously. Therefore, we will finally write:

$$\Delta Y = \Delta Y^{(1)} + \Delta Y^{(2)} + \Delta Y^{(3)} + \dots =$$

 $= 1 + [b(1-t) + t] + [b(1-t) + t]^{2} + [b(1-t) + t]^{3} + \cdots$ In a normal situation, 0 < b < 1 and 0 < t < 1. On the strength of this,

0 < [b(1-t)+t] = [b+(1-b)t] < [b+(1-b)] = 1.

Consequently, the derived series is an infinitely decreasing geometric progression, and the following equality is valid:

 $\Delta Y = [1 - b(1 - t) - t]^{-1} = \lambda_2.$

As we see, the main role in the multiplier process of creating equilibrium output is played by the joint marginal propensity of households and the government to purchase goods and services [b(1 - t) + t]. This parameter is the weighted value of two types of marginal propensity. One of them -b – is the marginal propensity of households to consume, and the other is the marginal propensity of the government to purchase products and services. In the model under consideration, the latter is equal to one, since, according to (12), each additional unit of net tax revenue is fully spent on government purchases. The two values of marginal propensity (b and 1) are weighted according to 1 - t and t. Since the marginal propensity for government purchases of products and services is greater than $b (0 \le b \le 1)$, the greater the value of t, the higher the joint marginal propensity [b(1-t)+t] will be. And this means that, in the case of a high average tax rate, a large part of the income goes into the market in the form of spending and, all else being equal, the level of equilibrium output is also high.

From what has been said, it follows that when the marginal propensity of households to consume is low in a country, and government purchases are planned in accordance with (12), then to stimulate aggregate demand and increase equilibrium output, it is advisable to raise the average tax rate. At the same time, it should be taken into account that implementing this measure will not affect the total amount of household consumption and will only increase the part of output that will go to providing for government purchases.

Version III of the Keynesian Model. We consider one more version of the Keynesian Model, which differs from Version II given above in how it describes the correlation between G and T. In particular, suppose that only a certain part of the net taxes going to the budget is used for purchases, and the rest is used to service government debt and create a reserve fund. In addition, we will assume that part of the government purchases is determined exogenously and does not depend on taxes. In such conditions, the correlation between G and T can be expressed by the following linear function:

$$G = gT + \tilde{G}_0, \qquad (16)$$

where \tilde{G}_0 is the autonomous value of government purchases the amount of which does not depend on taxes and is determined exogenously. In conditions of insufficient tax revenues, this part of purchases can be made through borrowing; and *g* is the marginal propensity for government purchases. This parameter should be seen as exogenously regulated. Based on the situation existing in the economy, the government can increase or decrease the value of *g*, but in any case the marginal propensity to purchase must satisfy the condition $0 \le g \le 1$, which is a fairly natural requirement.

In model (1)–(6), we replace the condition $G = G_0$ with (16) and call the system thus obtained *Version III of the Keynesian Model*. It is easy to establish that, according to this version, equilibrium output is determined by the following equation:

$$Y = \lambda_3 A_3 \,, \tag{17}$$

where:

$$A_3 = a + I_0 + \tilde{G}_0 + NX_0, \qquad (18)$$

$$\lambda_3 = \frac{1}{1 - b(1 - t) - gt} = \frac{1}{(1 - b) - t(g - b)}.$$
 (19)

As we see, in this model it is not the total amount of government purchases G that participates in the creation of autonomous spending A_3 , along with the elements a, I_0 , and NX_0 , as is traditional in the Keynesian Model of aggregate demand, but a part of this amount \tilde{G}_0 : autonomous government purchases, that is, purchases whose amount does not depend on net taxes going to the budget. Consequently, the autonomous spending multiplier λ_3 is also different. The latter is determined by the joint marginal propensity of households and government to purchase products and services [b(1-t)+gt], which is the weighted average of b and g. Comparing (9), (15), and (19), we notice that the multipliers λ_1 and λ_2 are particular cases of λ_3 . Specifically, λ_1 is derived from λ_3 in the case when g – the marginal propensity for government purchases - is equal to zero (zero marginal propensity to purchase does not mean that no purchases are made); and if g = 1 in (19), then λ_3 turns into λ_2 .

Previously, when considering Versions I and II of the Keynesian Model, it was shown that changes in the average tax rate *t* affect equilibrium output differently in the cases when g = 0 and g = 1. Generalization of this fact gives us (17)–(19), from which it follows that in the Keynesian Model the role of the average tax rate is determined by the relationship between the marginal propensity to consume *b* and the marginal propensity for government purchases *g*. When b > g, a rise in the average tax rate lowers the joint propensity of households and the government to purchase products and services [b(1 - t) + gt]. Therefore, all else being equal, an increase in *t* causes a reduction in equilibrium output. And in the opposite case (i.e., when b < g), an increase in the average tax rate causes growth of the joint marginal propensity of households and the government to purchase products and services, which, all else being equal, is a condition that fosters the growth of aggregate demand and, consequently, equilibrium output. And finally, when b = g, then both the joint marginal propensity of households and the government to purchase products and services and aggregate demand are indifferent to *t*.

From the analysis done using the versions of the Keynesian Model examined above, we can draw the following conclusion. The effect of an increase (or decrease) in the average tax rate and taxes as a whole on aggregate demand is not unequivocally negative (or positive), as it is customarily presented in canonical form in contemporary macroeconomics [1, ch. 3; 2, ch. 9; 3, ch. 12; 4, ch. 5]. Depending on what the values of the marginal propensity to consume b and the marginal propensity to purchase g are, in the general case a tax increase can cause either a reduction or growth of aggregate demand. At the same time, since g is a parameter that the government can easily regulate, by selecting its appropriate value the government can purposefully use a tax increase to conduct a stimulating or inhibiting economic policy.

ეკონომიკა

გასაშუალოებული საგადასახადო ტვირთის ზეგავლენა ერთობლივ მოთხოვნაზე (კეინზიანური მოდელები)

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სტატიაში საქონლის ბაზრის სტანდარტული კეინზიანური მოღელის გარდაქმნილი გარიანტის ანალიზის საფუძველზე დასაბუთებულია, რომ ერთობლივ მოთხოვნაზე საშუალო საგადასახადო განაკვეთის და მთლიანობაში გადასახადების ზრდის (კლების) ზემოქმედება ისე ცალსახად უარყოფითად (დადებითად) არ არის განსაზღვრული, როგორც ეს კანონიკური სახით თანამედროვე მაკროეკონომიკსშია მიღებული. იმაზე დამოკიდებულებით, თუ როგორია მოხმარებისადმი შინამეურნეობების მიღრეკილების და შესყიდვებისადმი სახელმწიფოს მიღრეკილების მნიშვნელობები, გადასახადების გადიდებამ ზოგად შემთხვევაში შეიძლება გამოიწვიოს ერთობლივი მოთხოვნის როგორც შემცირება, ისე გადიდება. ამასთან, რადგანაც შესყიდვებისადმი ზღვრული მიდრეკილება სახელმწიფოს მხრიდან თავისუფლად რეგულირებადი პარამეტრია, ამიტომ მისი შესაბამისი მნიშვნელობის არჩევით გადასახადების ზრდა მთავრობის მხრიდან მიზანმიმართულად შეიძლება გამოყენებულ იქნას როგორც წამახალისებელი, ისე დამმუხრუჭებელი ეკონომიკური პოლიტიკის გასატარებლად.

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